

Review - Integration/Particle Motion

Evaluate the indefinite integral.

1. $\int x\sqrt{x+2} dx$
2. $\int 6a^4(2a^5-1)^3 da$
3. $\int (3x^2-x)^4(12x-2) dx$
4. $\int 3x^3\sqrt{1-x^2} dx$
5. $\int \frac{2x^2}{\sqrt{1+x^3}} dx$
6. $\int \tan^4 x \sec^2 x dx$
7. $\int \frac{\sin x}{\cos^3 x} dx$
8. $\int (x^2+1)(x^3+3x)^4 dx$
9. $\int \frac{\sin\sqrt{x}}{\sqrt{x}} dx$

Evaluate the definite integral.

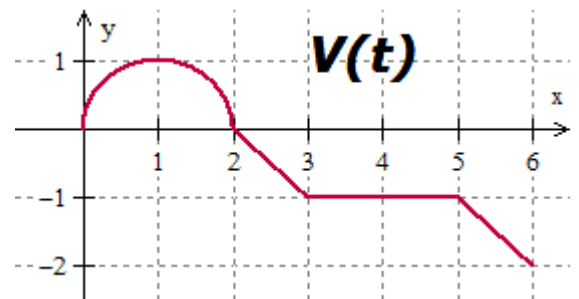
10. $\int_0^2 5x(3x^2-1)^3 dx$
11. $\int_1^4 \frac{x}{\sqrt{x}} dx$
12. $\int_3^5 \frac{2x}{\sqrt{2x-6}} dx$
13. $\int_1^2 x\sqrt{x-1} dx$
14. $\int_0^1 y(y^2+1)^5 dy$

Particle Motion

15. The velocity of the particle traveling on the x-axis over a 6 second time interval is shown at the right.

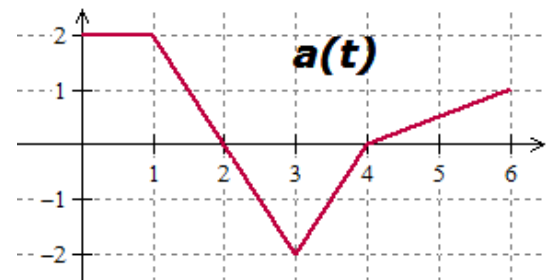
The position at time $t = 0$ is 1.

- a. Name the particles acceleration at $t = 1$ $t = 2.567$
- b. What is the particle's position at $t = 2$ $t = 6$
- c. Is the speed of the particle increasing or decreasing at $t = 5.5$? Explain!
- d. What is the particle's minimum position? When does it occur?
- e. What is the average acceleration from $t = 0$ to $t = 6$?
- f. Name the particle's average velocity from $t = 0$ to $t = 6$?



16. The acceleration of a particle traveling on the x-axis over a 6 second time interval is shown at the right. The velocity is -2 at $t = 0$.

- a. What is the velocity at $t = 1$ $t = 6$
- b. Is the speed of the particle increasing or decreasing at $t = 5$? Explain!
- c. What is the particle's minimum velocity? When does it occur?
- d. What is the average acceleration from $t = 0$ to $t = 6$?



17. A particle moves along the x-axis in such a way that the acceleration at time t for $t > 0$ is given by $a(t) = 2t$. When $t = 1$, the position of the particle is 2 and the velocity is 5.

- a. Write an equation for the velocity, $v(t)$, of the particle for all $t > 0$.
- b. Write an equation of the position, $x(t)$ of the particle for all $t > 0$.
- c. Find the velocity when the acceleration is 3.
- d. Find the average acceleration from $t = 0$ to $t = 2$.

18. Name 2 ways that you **COULD** find the average velocity. Show the correct equations but **do not solve**.

CALCULATOR – Show the calculation that leads to your answer!

A velocity of a particle as it moves along the x-axis is described by $v(t) = 3\sin(0.5x^2 + 1.6)$ from $t = 0$ seconds to $t = 3$ seconds. The starting position of the particle is 2.

- When is the particle moving right?
- Find the particle's acceleration at $t=2$.
- Is the particle speeding up or slowing down at $t = 2$. EXPLAIN.
- When is the particle at rest?
- What is the total distance that the particle covers in the 3 seconds?
- What is the average velocity of the particle during the 3 seconds?
- What is the average acceleration of the particle over the 3 seconds?
- What is the particle's position at $t = 3$?
- Draw a labeled picture of the particle's movement in the box. Show the calculations.
- What is the closest distance that the particle gets to $x = 8$? When is it there?

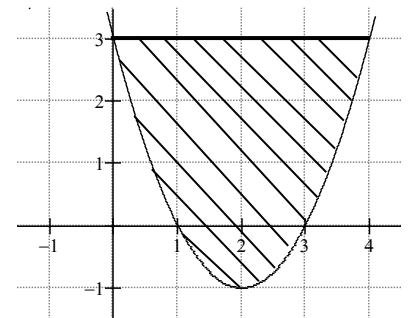
19. Find the area of the striped region for $f(x) = x^2 - 4x + 3$ pictured.

20-21 Find the area that is between function and the x – axis and the curve on the given interval without a calculator. You may check your answer with a calculator.

20. $f(x) = x^2 + 2x$, $[-3,0]$

21. $g(x) = \sin x$, $[0,2\pi]$

22. Find k such that $\int_1^k 3x^2 + 2x \, dx = -2$



Answers Review - Particle Motion

1. $\frac{2}{15}(x+2)^{\frac{3}{2}}(3x-4) + c$

2. $\frac{3}{20}(2a^5 - 1)^4 + c$

3. $\frac{2}{5}(3x^2 - x)^5 + c$

4. $-\frac{9}{8}(1-x^2)^{\frac{4}{3}} + c$

5. $\frac{4}{3}\sqrt{x^3 + 1} + c$

6. $\frac{1}{5}\tan^5 x + c$

7. $\frac{1}{2}\sec^2 x + c$

8. $\frac{1}{15}(x^3 + 3x)^5 + c$

9. $-2\cos\sqrt{x} + c$

10. 3050

11. $14/3$

12. $44/3$

13. $16/15$

14. $21/4$

15. -

a. 0, -1

b. $1 + \frac{\pi}{2}, -3 + \frac{\pi}{2}$

c. Vel neg, acc neg; speed increasing

d. $-3 + \frac{\pi}{2}$ at $t = 6$

e. $-1/3$

f. $\frac{\pi}{12} - \frac{2}{3}$

16. -

a. 0, 0

b. VEL NEG, ACC POS; SPEED IS DECREASING

c. MIN VELOCITY AT $t = 0$ and vel is -2

d. $1/3$

17. -

a. $v = t^2 + 4$

b. $pos = \frac{1}{3}t^3 + 4t - \frac{7}{3}$

c. At $t = 3/2$, vel is $25/4$

d. 2

e. $\frac{1}{b-a} \int_a^b v(t) dt$ OR $\frac{P(b) - P(a)}{b-a}$

18. -

a. (0, 1.756)

b. -5.381

c. NEG VEL, NEG ACC; SPEEDING UP

d. 1.756

e. 6.513

f. 0.547

g. -1.182

h. 3.642

i. -

j. At $t = 1.756$ the particle is 1.922 away from $x = 8$

19. $32/3$

20. $8/3$

21. 4

22. -1, 0